

## Homework 5

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**Last name:** \_\_\_\_\_  
**First name:** \_\_\_\_\_  
**Section:** \_\_\_\_\_

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*Due at the beginning of the class on **Wednesday** November 9th, 2016.*

**Exercise 1.** Find the general solution to

1.  $y'' + 7y' + 6y = 3 \sin 2x$ .

2.  $y'' + 6y' + 8y = 2t - 3$ .

3.  $y'' - y' - 2y = 2e^{-t}$ .

4.  $y'' - 4y' + 4y = x^{-3}e^{2x}$

5.  $y'' + 9y = \sec^3(3t)$ .

6.  $y'' + 16y = e^{-4x} + 3 \sin 4x$ .

**Exercise 2.** Find the solution to the initial value problem

$$y'' - 2y' + y = t^2, \quad y(0) = 1, \quad y'(0) = 0.$$

**Exercise 3.** Given that  $y_1 = t^{-1}$  is solution to the homogeneous equation

$$t^2 y'' + 3ty' + y = 0 \quad t > 0.$$

1. Use the method of reduction of order to find the general solution to the homogeneous equation.

2. Use the variation of parameters to find the general solution to

$$t^2 y'' + 3ty' + y = \frac{1}{t}, \quad t > 0.$$